Package: backbone (via r-universe)

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```
Title Extracts the Backbone from Graphs
Version 2.1.3
Description An implementation of methods for extracting an unweighted
     unipartite graph (i.e. a backbone) from an unweighted
     unipartite graph, a weighted unipartite graph, the projection
     of an unweighted bipartite graph, or the projection of a
     weighted bipartite graph (Neal, 2022
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```

Type Package

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Description

Provides methods for extracting from an unweighted and sparse subgraph (i.e., a backbone) that contains only the most "important" edges in a weighted bipartite projection, a non-projection weighted network, or an unweighted network.

Available backbone extraction functions include:

- For weighted bipartite projections of weighted bipartite networks: osdsm().
- For weighted bipartite projections of binary bipartite networks: fixedfill(), fixedrow(), fixedcol(), sdsm(), and fdsm().
- For non-projection weighted networks: global(), disparity().

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• For unweighted networks: sparsify(), sparsify.with.skeleton(), sparsify.with.gspar(), sparsify.with.lspar(), sparsify.with.simmelian(), sparsify.with.jaccard(), sparsify.with.meetmin() sparsify.with.geometric(), sparsify.with.localdegree(), sparsify.with.quadrilateral().

• For all networks: backbone.suggest() will examine the data and suggest an appropriate backbone function

The package also includes some utility functions:

- fastball() Fast marginal-preserving randomization of binary matrices
- bicm() Compute probabilities under the bipartite configuration model

For additional documentation and background on the package functions, see vignette("backbone"). For updates, papers, presentations, and other backbone news, please see www.rbackbone.net

References

Neal, Z. P. (2022). backbone: An R Package to Extract Network Backbones. *PLOS ONE*, *17*, e0269137. doi:10.1371/journal.pone.0269137

backbone.extract

Extracts a backbone network from a backbone object

Description

backbone.extract returns a binary or signed adjacency matrix containing the backbone that retains only the significant edges.

Usage

```
backbone.extract(
  bb.object,
  signed = FALSE,
  alpha = 0.05,
  mtc = "none",
  class = bb.object$class,
  narrative = FALSE
)
```

Arguments

bb.object backbone: backbone S3 class object.
signed boolean: TRUE for a signed backbone

boolean: TRUE for a signed backbone, FALSE for a binary backbone (see de-

tails)

alpha real: significance level of hypothesis test(s)

mtc string: type of Multiple Test Correction to be applied; can be any method al-

lowed by p.adjust.

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class string: the class of the returned backbone graph, one of c("matrix", "sparseMa-

trix", "igraph", "edgelist"), converted via tomatrix.

narrative boolean: TRUE if suggested text & citations should be displayed.

Details

The "backbone" S3 class object is composed of (1) the weighted graph as a matrix, (2) upper-tail p-values as a matrix, (3, if signed = TRUE) lower-tail p-values as a matrix, (4, if present) node attributes as a dataframe, and (5) several properties of the original graph and backbone model

When signed = FALSE, a one-tailed test (is the weight stronger?) is performed for each edge. The resulting backbone contains edges whose weights are significantly *stronger* than expected in the null model. When signed = TRUE, a two-tailed test (is the weight stronger or weaker?) is performed for each edge. The resulting backbone contains positive edges for those whose weights are significantly *stronger*, and negative edges for those whose weights are significantly *weaker*, than expected in the null model.

Value

backbone graph: Binary or signed backbone graph of class given in parameter class.

Examples

backbone.suggest

Suggest a backbone model

Description

backbone. suggest suggests and optionally runs an appropriate backbone model for a graph object.

Usage

```
backbone.suggest(G, s = NULL)
```

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Arguments

G	graph: A graph represented in an object of class matrix, sparse Matrix, dataframe, or igraph.
	of 1graph.
S	numeric: If provided, a backbone is extracted using this value as the significance

Value

If s == NULL: NULL, but a message is displayed with a suggested model. If 0 <= s <= 1: A binary backbone graph in the same class as G, obtained by extracting the backbone at the s significance level (if a statistical model is suggested) or using sparisfication parameter s (if a sparsification model is suggested). The code used to perform the extraction, and suggested manuscript text are displayed.

References

```
Neal, Z. P. (2022). backbone: An R Package to Extract Network Backbones. PLOS ONE, 17, e0269137. doi:10.1371/journal.pone.0269137
```

Examples

```
M <- matrix(runif(100),10,10) #A random weighted, directed graph
backbone <- backbone.suggest(M)
backbone <- backbone.suggest(M, s = 0.05)
```

level or sparsification parameter.

bicm

Bipartite Configuration Model

Description

bicm estimates cell probabilities under the bipartite configuration model

Usage

```
bicm(M, fitness = FALSE, tol = 1e-08, max_steps = 200, ...)
```

Arguments

М	matrix: a binary matrix
fitness	boolean: FALSE returns a matrix of probabilities, TRUE returns a list of row and column fitnesses only
tol	numeric, tolerance of algorithm
max_steps	numeric, number of times to run loglikelihood_prime_bicm algorithm
	optional arguments

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Details

Given a binary matrix **M**, the Bipartite Configuration Model (BiCM; Saracco et. al. 2015) returns a valued matrix **B** in which Bij is the *approximate* probability that Mij = 1 in the space of all binary matrices with the same row and column marginals as **M**. The BiCM yields the closest approximations of the true probabilities compared to other estimation methods (Neal et al., 2021), and is used by sdsm() to extract the backbone of a bipartite projection using the stochastic degree sequence model.

Matrix **M** is "conforming" if no rows and no columns contain only zeros or only ones. If **M** is conforming, then bicm() is faster. Additionally, if fitness = TRUE, then bicm() returns a list of row and column fitnesses, which requires less memory. Given the ith row's fitness Ri and the jth column's fitness Rj, the entry Bij in the probability matrix can be computed as Ri x Rj/(1+(Ri x Rj)).

Matrix **M** is "non-conforming" if any rows or any columns contain only zeros or only ones. If **M** is non-conforming, then bicm() is slower and will only return a probability matrix.

Value

a matrix of probabilities or a list of fitnesses

References

package: Neal, Z. P. (2022). backbone: An R Package to Extract Network Backbones. *PLOS ONE*, 17, e0269137. doi:10.1371/journal.pone.0269137

bicm: Saracco, F., Di Clemente, R., Gabrielli, A., & Squartini, T. (2015). Randomizing bipartite networks: The case of the World Trade Web. *Scientific Reports*, 5, 10595. doi:10.1038/srep10595

Examples

```
M \leftarrow matrix(c(0,0,1,0,1,0,1),3,3) #A binary matrix bicm(M)
```

disparity

Extract backbone using the Disparity Filter

Description

disparity extracts the backbone of a weighted network using the Disparity Filter.

Usage

```
disparity(
   W,
   alpha = 0.05,
   missing.as.zero = FALSE,
   signed = FALSE,
   mtc = "none",
```

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```
class = "original",
narrative = FALSE
)
```

Arguments

W A positively-weighted unipartite graph, as: (1) an adjacency matrix in the form

of a matrix or sparse Matrix; (2) an edgelist in the form of a three-column

dataframe; (3) an igraph object.

alpha real: significance level of hypothesis test(s)

missing.as.zero

boolean: should missing edges be treated as edges with zero weight and tested

for significance

signed boolean: TRUE for a signed backbone, FALSE for a binary backbone (see de-

tails)

mtc string: type of Multiple Test Correction to be applied; can be any method al-

lowed by p.adjust.

class string: the class of the returned backbone graph, one of c("original", "matrix",

"Matrix", "igraph", "edgelist"). If "original", the backbone graph returned is of

the same class as W.

narrative boolean: TRUE if suggested text & citations should be displayed.

Details

The disparity function applies the disparity filter (Serrano et al., 2009), which compares an edge's weight to its expected weight if a node's total degree was uniformly distributed across all its edges. The graph may be directed or undirected, however the edge weights must be positive.

When signed = FALSE, a one-tailed test (is the weight stronger?) is performed for each edge. The resulting backbone contains edges whose weights are significantly *stronger* than expected in the null model. When signed = TRUE, a two-tailed test (is the weight stronger or weaker?) is performed for each edge. The resulting backbone contains positive edges for those whose weights are significantly *stronger*, and negative edges for those whose weights are significantly *weaker*, than expected in the null model.

If W is an unweighted bipartite graph, then the disparity filter is applied to its weighted bipartite projection.

Value

If alpha != NULL: Binary or signed backbone graph of class class.

If alpha == NULL: An S3 backbone object containing (1) the weighted graph as a matrix, (2) upper-tail p-values as a matrix, (3, if signed = TRUE) lower-tail p-values as a matrix, (4, if present) node attributes as a dataframe, and (5) several properties of the original graph and backbone model, from which a backbone can subsequently be extracted using backbone.extract().

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References

package: Neal, Z. P. (2022). backbone: An R Package to Extract Network Backbones. *PLOS ONE*, 17, e0269137. doi:10.1371/journal.pone.0269137

disparity filter: Serrano, M. A., Boguna, M., & Vespignani, A. (2009). Extracting the multiscale backbone of complex weighted networks. *Proceedings of the National Academy of Sciences*, 106, 6483-6488. doi:10.1073/pnas.0808904106

Examples

```
#A network with heterogeneous (i.e. multiscale) weights
10,0,1,1,1,0,0,0,0,0,0,
               10,1,0,1,1,0,0,0,0,0,
               10,1,1,0,1,0,0,0,0,0,0,
               10,1,1,1,0,0,0,0,0,0,0,
                75,0,0,0,0,0,100,100,100,100,
                0,0,0,0,0,100,0,10,10,10,
                0,0,0,0,0,100,10,0,10,10,
                0,0,0,0,0,100,10,10,0,10,
                0,0,0,0,0,100,10,10,10,0),10)
net <- igraph::graph_from_adjacency_matrix(net, mode = "undirected", weighted = TRUE)</pre>
plot(net, edge.width = sqrt(igraph::E(net)$weight)) #A stronger clique & a weaker clique
strong <- igraph::delete.edges(net, which(igraph::E(net)$weight < mean(igraph::E(net)$weight)))</pre>
plot(strong) #A backbone of stronger-than-average edges ignores the weaker clique
bb <- disparity(net, alpha = 0.05, narrative = TRUE) #A disparity backbone...
plot(bb) #...preserves edges at multiple scales
```

fastball

Randomize a binary matrix using the fastball algorithm

Description

fastball randomizes a binary matrix, preserving the row and column sums

Usage

```
fastball(M, trades = 5 * nrow(M))
```

Arguments

M matrix: a binary matrix (see details)

trades integer: number of trades; the default is 5R trades (approx. mixing time)

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Details

Given a matrix M, fastball randomly samples a new matrix from the space of all matrices with the same row and column sums as M.

Value

matrix: A random binary matrix with same row sums and column sums as M.

References

fastball: Godard, Karl and Neal, Zachary P. 2022. fastball: A fast algorithm to sample bipartite graphs with fixed degree sequences. *Journal of Complex Networks* doi:10.1093/comnet/cnac049

Examples

```
M <- matrix(rbinom(200,1,0.5),10,20) #A random 10x20 binary matrix Mrand <- fastball(M) #Random matrix with same row and column sums
```

fdsm

Extract backbone using the Fixed Degree Sequence Model

Description

fdsm extracts the backbone of a bipartite projection using the Fixed Degree Sequence Model.

Usage

```
fdsm(
   B,
   alpha = 0.05,
   trials = NULL,
   missing.as.zero = FALSE,
   signed = FALSE,
   mtc = "none",
   class = "original",
   narrative = FALSE,
   progress = TRUE,
   ...
)
```

Arguments

B An unweighted bipartite graph, as: (1) an incidence matrix in the form of a matrix or sparse Matrix; (2) an edgelist in the form of a two-column dataframe;

(3) an igraph object.

alpha real: significance level of hypothesis test(s)

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trials numeric: the number of bipartite graphs generated to approximate the edge

weight distribution. If NULL, the number of trials is selected based on alpha

(see details)

missing.as.zero

boolean: should missing edges be treated as edges with zero weight and tested

for significance

signed boolean: TRUE for a signed backbone, FALSE for a binary backbone (see de-

tails)

mtc string: type of Multiple Test Correction to be applied; can be any method al-

lowed by p.adjust.

class string: the class of the returned backbone graph, one of c("original", "matrix",

"Matrix", "igraph", "edgelist"). If "original", the backbone graph returned is of

the same class as B.

narrative boolean: TRUE if suggested text & citations should be displayed.

progress boolean: TRUE if the progress of Monte Carlo trials should be displayed.

... optional arguments

Details

The fdsm function compares an edge's observed weight in the projection B*t(B) to the distribution of weights expected in a projection obtained from a random bipartite network where both the row vertex degrees and column vertex degrees are *exactly* fixed at their values in B. It uses the fastball() algorithm to generate random bipartite matrices with give row and column vertex degrees.

When signed = FALSE, a one-tailed test (is the weight stronger?) is performed for each edge. The resulting backbone contains edges whose weights are significantly *stronger* than expected in the null model. When signed = TRUE, a two-tailed test (is the weight stronger or weaker?) is performed for each edge. The resulting backbone contains positive edges for those whose weights are significantly *stronger*, and negative edges for those whose weights are significantly *weaker*, than expected in the null model.

The p-values used to evaluate the statistical significance of each edge are computed using Monte Carlo methods. The number of trials performed affects the precision of these p-values. This precision impacts the confidence that a given edge's p-value is less than the desired alpha level, and therefore represents a statistically significant edge that should be retained in the backbone. When trials = NULL, trials.needed() is used to estimate the required number of trials to evaluate the statistical significance of an edges' p-values.

Value

If alpha != NULL: Binary or signed backbone graph of class class.

If alpha == NULL: An S3 backbone object containing (1) the weighted graph as a matrix, (2) upper-tail p-values as a matrix, (3, if signed = TRUE) lower-tail p-values as a matrix, (4, if present) node attributes as a dataframe, and (5) several properties of the original graph and backbone model, from which a backbone can subsequently be extracted using backbone.extract().

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References

package: Neal, Z. P. (2022). backbone: An R Package to Extract Network Backbones. *PLOS ONE*, 17, e0269137. doi:10.1371/journal.pone.0269137

fdsm: Neal, Z. P., Domagalski, R., and Sagan, B. (2021). Comparing Alternatives to the Fixed Degree Sequence Model for Extracting the Backbone of Bipartite Projections. *Scientific Reports*. doi:10.1038/s41598021032383

fastball: Godard, Karl and Neal, Zachary P. 2022. fastball: A fast algorithm to sample bipartite graphs with fixed degree sequences. *Journal of Complex Networks* doi:10.1093/comnet/cnac049

Examples

fixedcol

Extract backbone using the Fixed Column Model

Description

fixedcol extracts the backbone of a bipartite projection using the Fixed Column Model.

Usage

```
fixedcol(
   B,
   alpha = 0.05,
   missing.as.zero = FALSE,
   signed = FALSE,
   mtc = "none",
   class = "original",
   narrative = FALSE
)
```

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Arguments

B An unweighted bipartite graph, as: (1) an incidence matrix in the form of a

matrix or sparse Matrix; (2) an edgelist in the form of a two-column dataframe;

(3) an igraph object.

alpha real: significance level of hypothesis test(s)

missing.as.zero

boolean: should missing edges be treated as edges with zero weight and tested

for significance

signed boolean: TRUE for a signed backbone, FALSE for a binary backbone (see de-

tails)

mtc string: type of Multiple Test Correction to be applied; can be any method al-

lowed by p.adjust.

class string: the class of the returned backbone graph, one of c("original", "matrix",

"Matrix", "igraph", "edgelist"). If "original", the backbone graph returned is of

the same class as B.

narrative boolean: TRUE if suggested text & citations should be displayed.

Details

This fixedcol function compares an edge's observed weight in the projection B * t(B) to the distribution of weights expected in a projection obtained from a random bipartite graph where the *column* vertex degrees are fixed but the row vertex degrees are allowed to vary.

When signed = FALSE, a one-tailed test (is the weight stronger?) is performed for each edge. The resulting backbone contains edges whose weights are significantly *stronger* than expected in the null model. When signed = TRUE, a two-tailed test (is the weight stronger or weaker?) is performed for each edge. The resulting backbone contains positive edges for those whose weights are significantly *stronger*, and negative edges for those whose weights are significantly *weaker*, than expected in the null model.

Value

If alpha != NULL: Binary or signed backbone graph of class class.

If alpha == NULL: An S3 backbone object containing (1) the weighted graph as a matrix, (2) upper-tail p-values as a matrix, (3, if signed = TRUE) lower-tail p-values as a matrix, (4, if present) node attributes as a dataframe, and (5) several properties of the original graph and backbone model, from which a backbone can subsequently be extracted using backbone.extract().

References

package: Neal, Z. P. (2022). backbone: An R Package to Extract Network Backbones. *PLOS ONE*, 17, e0269137. doi:10.1371/journal.pone.0269137

fixedcol: Neal, Z. P., Domagalski, R., and Sagan, B. (2021). Comparing Alternatives to the Fixed Degree Sequence Model for Extracting the Backbone of Bipartite Projections. *Scientific Reports*, 11, 23929. doi:10.1038/s41598021032383

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Examples

fixedfill

Extract backbone using the Fixed Fill Model

Description

fixedfill extracts the backbone of a bipartite projection using the Fixed Fill Model.

Usage

```
fixedfill(
   B,
   alpha = 0.05,
   missing.as.zero = FALSE,
   signed = FALSE,
   mtc = "none",
   class = "original",
   narrative = FALSE
)
```

Arguments

В

An unweighted bipartite graph, as: (1) an incidence matrix in the form of a matrix or sparse Matrix; (2) an edgelist in the form of a two-column dataframe; (3) an igraph object.

alpha

real: significance level of hypothesis test(s)

missing.as.zero

boolean: should missing edges be treated as edges with zero weight and tested for significance

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signed	boolean: TRUE for a signed backbone, FALSE for a binary backbone (see details)
mtc	string: type of Multiple Test Correction to be applied; can be any method allowed by p.adjust.
class	string: the class of the returned backbone graph, one of c("original", "matrix", "Matrix", "igraph", "edgelist"). If "original", the backbone graph returned is of the same class as B.
narrative	boolean: TRUE if suggested text & citations should be displayed.

Details

The fixedfill function compares an edge's observed weight in the projection B * t(B) to the distribution of weights expected in a projection obtained from a random bipartite graph where the number of edges present (i.e., the number of cells *filled* with a 1) is equal to the number of edges in B. When B is large, this function may be impractically slow and may return a backbone object that contains NaN values.

When signed = FALSE, a one-tailed test (is the weight stronger?) is performed for each edge. The resulting backbone contains edges whose weights are significantly *stronger* than expected in the null model. When signed = TRUE, a two-tailed test (is the weight stronger or weaker?) is performed for each edge. The resulting backbone contains positive edges for those whose weights are significantly *stronger*, and negative edges for those whose weights are significantly *weaker*, than expected in the null model.

Value

If alpha != NULL: Binary or signed backbone graph of class class.

If alpha == NULL: An S3 backbone object containing (1) the weighted graph as a matrix, (2) upper-tail p-values as a matrix, (3, if signed = TRUE) lower-tail p-values as a matrix, (4, if present) node attributes as a dataframe, and (5) several properties of the original graph and backbone model, from which a backbone can subsequently be extracted using backbone.extract().

References

```
package: Neal, Z. P. (2022). backbone: An R Package to Extract Network Backbones. PLOS ONE, 17, e0269137. doi:10.1371/journal.pone.0269137
```

fixedfill: Neal, Z. P., Domagalski, R., and Sagan, B. (2021). Comparing Alternatives to the Fixed Degree Sequence Model for Extracting the Backbone of Bipartite Projections. *Scientific Reports*, 11, 23929. doi:10.1038/s41598021032383

Examples

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fixedrow

Extract backbone using the Fixed Row Model

Description

fixedrow extracts the backbone of a bipartite projection using the Fixed Row Model.

Usage

```
fixedrow(
   B,
   alpha = 0.05,
   missing.as.zero = FALSE,
   signed = FALSE,
   mtc = "none",
   class = "original",
   narrative = FALSE
)
```

Arguments

B An unweighted bipartite graph, as: (1) an incidence matrix in the form of a matrix or sparse Matrix; (2) an edgelist in the form of a two-column dataframe;

(3) an igraph object.

alpha real: significance level of hypothesis test(s)

missing.as.zero

boolean: should missing edges be treated as edges with zero weight and tested

for significance

signed boolean: TRUE for a signed backbone, FALSE for a binary backbone (see de-

tails)

mtc string: type of Multiple Test Correction to be applied; can be any method al-

lowed by p.adjust.

class string: the class of the returned backbone graph, one of c("original", "matrix",

"Matrix", "igraph", "edgelist"). If "original", the backbone graph returned is of

the same class as B.

narrative boolean: TRUE if suggested text & citations should be displayed.

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Details

The fixedrow function compares an edge's observed weight in the projection B * t(B) to the distribution of weights expected in a projection obtained from a random bipartite graph where the *row* vertex degrees are fixed but the column vertex degrees are allowed to vary.

When signed = FALSE, a one-tailed test (is the weight stronger?) is performed for each edge. The resulting backbone contains edges whose weights are significantly *stronger* than expected in the null model. When signed = TRUE, a two-tailed test (is the weight stronger or weaker?) is performed for each edge. The resulting backbone contains positive edges for those whose weights are significantly *stronger*, and negative edges for those whose weights are significantly *weaker*, than expected in the null model.

Value

If alpha != NULL: Binary or signed backbone graph of class class.

If alpha == NULL: An S3 backbone object containing (1) the weighted graph as a matrix, (2) upper-tail p-values as a matrix, (3, if signed = TRUE) lower-tail p-values as a matrix, (4, if present) node attributes as a dataframe, and (5) several properties of the original graph and backbone model, from which a backbone can subsequently be extracted using backbone.extract().

References

package: Neal, Z. P. (2022). backbone: An R Package to Extract Network Backbones. *PLOS ONE*, 17, e0269137. doi:10.1371/journal.pone.0269137

Neal, Z. P., Domagalski, R., and Sagan, B. (2021). Comparing Alternatives to the Fixed Degree Sequence Model for Extracting the Backbone of Bipartite Projections. *Scientific Reports*, *11*, 23929. doi:10.1038/s41598021032383

Examples

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Compute global threshold backbone

Description

global extracts the backbone of a weighted network using a global threshold

Usage

```
global(
   G,
   upper = 0,
   lower = NULL,
   keepzeros = TRUE,
   class = "original",
   narrative = FALSE
)
```

Arguments

G	A weighted unipartite graph, as: (1) an adjacency matrix in the form of a matrix or sparse Matrix, or dataframe; (2) an edgelist in the form of a three-column dataframe; (3) an igraph object.
upper	real, FUN, or NULL: upper threshold value or function that evaluates to an upper threshold value.
lower	real, FUN, or NULL: lower threshold value or function that evaluates to a lower threshold value.
keepzeros	boolean: TRUE if zero-weight edges in W should be excluded from (i.e. also be zero in) the backbone
class	string: the class of the returned backbone graph, one of c("original", "matrix", "Matrix", "igraph", "edgelist"). If "original", the backbone graph returned is of the same class as W.
narrative	boolean: TRUE if suggested text & citations should be displayed.

Details

The global function retains a edge with weight W if W > upper. If a lower threshold is also specified, it returns a signed backbone in which an edge's weight is set to 1 if W > upper, is set to -1 if W < lower, and is set to 0 otherwise. The default is an unsigned backbone containing all edges with non-zero weights.

If G is an unweighted bipartite graph, the global threshold is applied to its weighted bipartite projection.

Value

Binary or signed backbone graph of class given in parameter class.

lans

References

package: Neal, Z. P. (2022). backbone: An R Package to Extract Network Backbones. *PLOS ONE*, 17, e0269137. doi:10.1371/journal.pone.0269137

model: Neal, Z. P. (2014). The backbone of bipartite projections: Inferring relationships from co-authorship, co-sponsorship, co-attendance, and other co-behaviors. *Social Networks*, *39*, 84-97. doi:10.1016/j.socnet.2014.06.001

Examples

lans

Extract backbone using Locally Adaptive Network Sparsification

Description

lans extracts the backbone of a weighted network using Locally Adaptive Network Sparsification

Usage

```
lans(
   W,
   alpha = 0.05,
   missing.as.zero = FALSE,
   signed = FALSE,
   mtc = "none",
   class = "original",
   narrative = FALSE
)
```

Arguments

W

A positively-weighted unipartite graph, as: (1) an adjacency matrix in the form of a matrix or sparse Matrix; (2) an edgelist in the form of a three-column dataframe; (3) an igraph object.

alpha real: significance level of hypothesis test(s)

missing.as.zero

boolean: should missing edges be treated as edges with zero weight and tested

for significance

signed

boolean: TRUE for a signed backbone, FALSE for a binary backbone (see de-

tails)

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mtc string: type of Multiple Test Correction to be applied; can be any method al-

lowed by p.adjust.

class string: the class of the returned backbone graph, one of c("original", "matrix",

"Matrix", "igraph", "edgelist"). If "original", the backbone graph returned is of

the same class as W.

narrative boolean: TRUE if suggested text & citations should be displayed.

Details

The lans function applies Locally Adaptive Network Sparsification (LANS; Foti et al., 2011), which compares an edge's fractional weight to the cumulative distribution function for the fractional edge weights of all edges connected to a given node. The graph may be directed or undirected, however the edge weights must be positive.

When signed = FALSE, a one-tailed test (is the weight stronger?) is performed for each edge. The resulting backbone contains edges whose weights are significantly *stronger* than expected in the null model. When signed = TRUE, a two-tailed test (is the weight stronger or weaker?) is performed for each edge. The resulting backbone contains positive edges for those whose weights are significantly *stronger*, and negative edges for those whose weights are significantly *weaker*, than expected in the null model.

If W is an unweighted bipartite graph, then LANS is applied to its weighted bipartite projection.

Value

If alpha != NULL: Binary or signed backbone graph of class class.

If alpha == NULL: An S3 backbone object containing (1) the weighted graph as a matrix, (2) upper-tail p-values as a matrix, (3, if signed = TRUE) lower-tail p-values as a matrix, (4, if present) node attributes as a dataframe, and (5) several properties of the original graph and backbone model, from which a backbone can subsequently be extracted using backbone.extract().

References

package: Neal, Z. P. (2022). backbone: An R Package to Extract Network Backbones. *PLOS ONE*, 17, e0269137. doi:10.1371/journal.pone.0269137

lans: Foti, N. J., Hughes, J. M., and Rockmore, D. N. (2011). Nonparametric Sparsification of Complex Multiscale Networks. *PLOS One*, *6*, e16431. doi:10.1371/journal.pone.0016431

Examples

20 logit

logit

Logit-based probabilities for SDSM

Description

logit estimates cell probabilities under the logit model

Usage

logit(M)

Arguments

М

matrix

Details

Given a matrix \mathbf{M} , the logit model returns a valued matrix \mathbf{B} in which Bij is the *approximate* probability that Mij = 1 in the space of all binary matrices with the same row and column marginals as \mathbf{M} .

The Bipartite Configuration Model (BiCM), which is available using bicm is faster and yields slightly more accurate probabilities (Neal et al., 2021). Therefore, it is the default used in sdsm. However, the BiCM it requires the assumption that any cell in **M** can take a value of 0 or 1.

In contrast, the logit model allows constraints on specific cells. If \mathbf{M} represents a bipartite graph, these constraints are equivalent to structural 0s (an edge that can never be present) and structural 1s (an edge that must always be present). To impose such constraints, \mathbf{M} should be binary, except that structural 0s are represented with Mij = 10, and structural 1s are represented with Mij = 11.

Value

a matrix of probabilities

References

package: Neal, Z. P. (2022). backbone: An R Package to Extract Network Backbones. *PLOS ONE*, 17, e0269137. doi:10.1371/journal.pone.0269137

logit model: Neal, Z. P. (2014). The backbone of bipartite projections: Inferring relationships from co-authorship, co-sponsorship, co-attendance and other co-behaviors. *Social Networks*, *39*, 84-97. doi:10.1016/j.socnet.2014.06.001

logit model with constraints: Neal, Z. P. and Neal, J. W. (2024). Stochastic Degree Sequence Model with Edge Constraints (SDSM-EC) for Backbone Extraction. *Proceedings of the 12th International Conference on Complex Networks and their Applications*. Springer.

mlf 21

Examples

mlf

Extract backbone using the Marginal Likelihood Filter

Description

mlf extracts the backbone of a weighted network using the Marginal Likelihood Filter

Usage

```
mlf(
    W,
    alpha = 0.05,
    missing.as.zero = FALSE,
    signed = FALSE,
    mtc = "none",
    class = "original",
    narrative = FALSE
)
```

Arguments

W An integer-weighted unipartite graph, as: (1) an adjacency matrix in the form

of a matrix or sparse Matrix; (2) an edgelist in the form of a three-column

dataframe; (3) an igraph object.

alpha real: significance level of hypothesis test(s)

missing.as.zero

boolean: should missing edges be treated as edges with zero weight and tested

for significance

signed boolean: TRUE for a signed backbone, FALSE for a binary backbone (see de-

tails)

mtc string: type of Multiple Test Correction to be applied; can be any method al-

lowed by p.adjust.

class string: the class of the returned backbone graph, one of c("original", "matrix",

"Matrix", "igraph", "edgelist"). If "original", the backbone graph returned is of

the same class as W.

narrative boolean: TRUE if suggested text & citations should be displayed.

22 mlf

Details

The mlf function applies the marginal likelihood filter (MLF; Dianati, 2016), which compares an edge's weight to its expected weight in a graph that preserves the total weight and preserves the degree sequence *on average*. The graph may be directed or undirected, however the edge weights must be positive integers.

When signed = FALSE, a one-tailed test (is the weight stronger?) is performed for each edge. The resulting backbone contains edges whose weights are significantly *stronger* than expected in the null model. When signed = TRUE, a two-tailed test (is the weight stronger or weaker?) is performed for each edge. The resulting backbone contains positive edges for those whose weights are significantly *stronger*, and negative edges for those whose weights are significantly *weaker*, than expected in the null model.

If W is an unweighted bipartite graph, then the MLF is applied to its weighted bipartite projection.

Value

If alpha != NULL: Binary or signed backbone graph of class class.

If alpha == NULL: An S3 backbone object containing (1) the weighted graph as a matrix, (2) upper-tail p-values as a matrix, (3, if signed = TRUE) lower-tail p-values as a matrix, (4, if present) node attributes as a dataframe, and (5) several properties of the original graph and backbone model, from which a backbone can subsequently be extracted using backbone.extract().

References

package: Neal, Z. P. (2022). backbone: An R Package to Extract Network Backbones. *PLOS ONE*, 17, e0269137. doi:10.1371/journal.pone.0269137

mlf: Dianati, N. (2016). Unwinding the hairball graph: Pruning algorithms for weighted complex networks. *Physical Review E*, *93*, 012304. doi:10.1103/PhysRevE.93.012304

Examples

```
#A network with heterogeneous weights
10,0,1,1,1,0,0,0,0,0,0,
               10,1,0,1,1,0,0,0,0,0,
               10,1,1,0,1,0,0,0,0,0,0,
               10,1,1,1,0,0,0,0,0,0,0,
               75,0,0,0,0,0,100,100,100,100,
               0,0,0,0,0,100,0,10,10,10,
               0,0,0,0,0,100,10,0,10,10,
               0,0,0,0,0,100,10,10,0,10,
               0,0,0,0,0,100,10,10,10,0),10)
net <- igraph::graph_from_adjacency_matrix(net, mode = "undirected", weighted = TRUE)</pre>
plot(net, edge.width = sqrt(igraph::E(net)$weight)) #A stronger clique & a weaker clique
strong <- igraph::delete.edges(net, which(igraph::E(net)$weight < mean(igraph::E(net)$weight)))</pre>
plot(strong) #A backbone of stronger-than-average edges ignores the weaker clique
bb <- mlf(net, alpha = 0.05, narrative = TRUE) #An MLF backbone...
```

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```
plot(bb) #...preserves edges at multiple scales
```

osdsm Extract backbone using the Ordinal Stochastic Degree Sequence Model

Description

osdsm extracts the backbone of a bipartite projection using the Ordinal Stochastic Degree Sequence Model.

Usage

```
osdsm(
   B,
   alpha = 0.05,
   trials = NULL,
   missing.as.zero = FALSE,
   signed = FALSE,
   mtc = "none",
   class = "original",
   narrative = FALSE,
   progress = TRUE,
   ...
)
```

Arguments

trials

В	An ordinally weighted bipartite graph, as: (1) an incidence matrix in the form
	of a matrix or sparse Matrix; (2) an edgelist in the form of a three-column
	dataframe; (3) an igraph object.
alpha	real: significance level of hypothesis test(s)

integer: the number of bipartite graphs generated to approximate the edge weight distribution. If NULL, the number of trials is selected based on alpha (see details)

_

missing.as.zero

boolean: should missing edges be treated as edges with zero weight and tested

for significance

signed boolean: TRUE for a signed backbone, FALSE for a binary backbone (see de-

tails)

mtc string: type of Multiple Test Correction to be applied; can be any method al-

lowed by p.adjust.

class string: the class of the returned backbone graph, one of c("original", "matrix",

"Matrix", "igraph", "edgelist"). If "original", the backbone graph returned is of

the same class as B.

24 osdsm

narrative boolean: TRUE if suggested text & citations should be displayed.

progress boolean: TRUE if the progress of Monte Carlo trials should be displayed.

optional arguments

Details

The osdsm function compares an edge's observed weight in the projection B*t(B) to the distribution of weights expected in a projection obtained from a random bipartite network where both the rows and the columns contain approximately the same number of each value. The edges in B must be integers, and are assumed to represent an ordinal-level measure such as a Likert scale that starts at 0

When signed = FALSE, a one-tailed test (is the weight stronger?) is performed for each edge. The resulting backbone contains edges whose weights are significantly *stronger* than expected in the null model. When signed = TRUE, a two-tailed test (is the weight stronger or weaker?) is performed for each edge. The resulting backbone contains positive edges for those whose weights are significantly *stronger*, and negative edges for those whose weights are significantly *weaker*, than expected in the null model.

The p-values used to evaluate the statistical significance of each edge are computed using Monte Carlo methods. The number of trials performed affects the precision of these p-values. This precision impacts the confidence that a given edge's p-value is less than the desired alpha level, and therefore represents a statistically significant edge that should be retained in the backbone. When trials = NULL, trials.needed() is used to estimate the required number of trials to evaluate the statistical significance of an edges' p-values.

Value

If alpha != NULL: Binary or signed backbone graph of class class.

If alpha == NULL: An S3 backbone object containing (1) the weighted graph as a matrix, (2) upper-tail p-values as a matrix, (3, if signed = TRUE) lower-tail p-values as a matrix, (4, if present) node attributes as a dataframe, and (5) several properties of the original graph and backbone model, from which a backbone can subsequently be extracted using backbone.extract().

References

```
package: Neal, Z. P. (2022). backbone: An R Package to Extract Network Backbones. PLOS ONE, 17, e0269137. doi:10.1371/journal.pone.0269137
```

osdsm: Neal, Z. P. (2017). Well connected compared to what? Rethinking frames of reference in world city network research. *Environment and Planning A*, 49, 2859-2877. doi:10.1177/0308518X16631339

Examples

pb 25

pb

Poisson binomial distribution function

Description

pb computes the poisson binomial distribution function using the refined normal approximation.

Usage

```
pb(k, p, lowertail = TRUE)
```

Arguments

k numeric: value where the pdf should be evaluated

p vector: vector of success probabilities

lowertail boolean: If TRUE return both upper & lower tail probabilities, if FALSE return

only upper tail probability

Details

The Refined Normal Approximation (RNA) offers a close approximation when length(p) is large (Hong, 2013).

Value

vector, length 2: The first value (if lower = TRUE) is the lower tail probability, the probability of observing k or fewer successes when each trial has probability p of success. The second value is the upper tail probability, the probability of observing k or more successes when each trial has probability p of success.

References

Hong, Y. (2013). On computing the distribution function for the Poisson binomial distribution. *Computational Statistics and Data Analysis*, 59, 41-51. doi:10.1016/j.csda.2012.10.006

Examples

```
pb(50,runif(100))
```

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sdsm

Extract backbone using the Stochastic Degree Sequence Model

Description

sdsm extracts the backbone of a bipartite projection using the Stochastic Degree Sequence Model.

Usage

```
sdsm(
   B,
   alpha = 0.05,
   missing.as.zero = FALSE,
   signed = FALSE,
   mtc = "none",
   class = "original",
   narrative = FALSE,
   ...
)
```

Arguments

An unweighted bipartite graph, as: (1) an incidence matrix in the form of a matrix or sparse Matrix; (2) an edgelist in the form of a two-column dataframe;

(3) an igraph object.

alpha real: significance level of hypothesis test(s)

missing.as.zero

boolean: should missing edges be treated as edges with zero weight and tested

for significance

signed boolean: TRUE for a signed backbone, FALSE for a binary backbone (see de-

tails)

mtc string: type of Multiple Test Correction to be applied; can be any method al-

lowed by p.adjust.

class string: the class of the returned backbone graph, one of c("original", "matrix",

"Matrix", "igraph", "edgelist"). If "original", the backbone graph returned is of

the same class as B.

narrative boolean: TRUE if suggested text & citations should be displayed.

... optional arguments

Details

The sdsm function compares an edge's observed weight in the projection B*t(B) to the distribution of weights expected in a projection obtained from a random bipartite network where both the row vertex degrees and column vertex degrees are *approximately* fixed at their values in B.

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When signed = FALSE, a one-tailed test (is the weight stronger?) is performed for each edge. The resulting backbone contains edges whose weights are significantly *stronger* than expected in the null model. When signed = TRUE, a two-tailed test (is the weight stronger or weaker?) is performed for each edge. The resulting backbone contains positive edges for those whose weights are significantly *stronger*, and negative edges for those whose weights are significantly *weaker*, than expected in the null model.

The bipartite network B may contain some edges that are *required* in the null model (i.e., structural 1s); these edges should have a weight of 11 (i.e., B_ik = 11). This network may also contain some edges that are *prohibited* in the null model (i.e., structural 0s); these edges should have a weight of 10 (i.e., B_ik = 10). When B contains required or prohibited edges, cellwise probabilities are computed using logit following Neal et al. (2024). Otherwise, cellwise probabilities are computed using the faster and more accurate Bipartite Configuration Model with bicm (Neal et al. 2021).

Value

If alpha != NULL: Binary or signed backbone graph of class class.

If alpha == NULL: An S3 backbone object containing (1) the weighted graph as a matrix, (2) upper-tail p-values as a matrix, (3, if signed = TRUE) lower-tail p-values as a matrix, (4, if present) node attributes as a dataframe, and (5) several properties of the original graph and backbone model, from which a backbone can subsequently be extracted using backbone.extract().

References

package: Neal, Z. P. (2022). backbone: An R Package to Extract Network Backbones. *PLOS ONE*, 17, e0269137. doi:10.1371/journal.pone.0269137

sdsm: Neal, Z. P. (2014). The backbone of bipartite projections: Inferring relationships from co-authorship, co-sponsorship, co-attendance, and other co-behaviors. *Social Networks*, *39*, 84-97. doi:10.1016/j.socnet.2014.06.001

bicm: Neal, Z. P., Domagalski, R., and Sagan, B. (2021). Comparing Alternatives to the Fixed Degree Sequence Model for Extracting the Backbone of Bipartite Projections. *Scientific Reports*, 11, 23929. doi:10.1038/s41598021032383

logit: Neal, Z. P. and Neal, J. W. (2024). Stochastic Degree Sequence Model with Edge Constraints (SDSM-EC) for Backbone Extraction. *Proceedings of the 12th International Conference on Complex Networks and their Applications*. Springer.

Examples

P <- B%*%t(B) #An ordinary weighted projection...

28 sparsify

sparsify

Extract the backbone from a network using a sparsification model

Description

A generic function to extract the backbone of an undirected, unipartite network using a sparsification model described by a combination of an edge scoring metric, a edge score normalization, and an edge score filter.

Usage

```
sparsify(
   U,
   s,
   escore,
   normalize,
   filter,
   symmetrize = TRUE,
   umst = FALSE,
   class = "original",
   narrative = FALSE
)
```

Arguments

U	An unweighted unipartite graph, as: (1) an adjacency matrix in the form of a matrix or sparse Matrix; (2) an edgelist in the form of a two-column dataframe; (3) an igraph object.
S	numeric: Sparsification parameter
escore	string: Method for scoring edges' importance
normalize	string: Method for normalizing edge scores
filter	string: Type of filter to apply
symmetrize	boolean: TRUE if the result should be symmetrized
umst	boolean: TRUE if the backbone should include the union of minimum spanning trees, to ensure connectivity
class	string: the class of the returned backbone graph, one of c("original", "matrix", "Matrix", "igraph", "edgelist"). If "original", the backbone graph returned is of the same class as \cup .
narrative	boolean: TRUE if suggested text & citations should be displayed.

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Details

The escore parameter determines how an unweighted edge's importance is calculated. Unless noted below, scores are symmetric and larger values represent more important edges.

- random: a random number drawn from a uniform distribution
- betweenness: edge betweenness
- triangles: number of triangles that include the edge
- jaccard: jaccard similarity coefficient of the neighborhoods of an edge's endpoints, or alternatively, triangles normalized by the size of the union of the endpoints neighborhoods
- dice: dice similarity coefficient of the neighborhoods of an edge's endpoints
- quadrangles: number of quadrangles that include the edge
- quadrilateral embeddedness: geometric mean normalization of quadrangles
- degree: degree of neighbor to which an edge is adjacent (asymmetric)
- meetmin: triangles normalized by the smaller of the endpoints' neighborhoods' sizes
- geometric: triangles normalized by the product of the endpoints' neighborhoods' sizes
- hypergeometric: probability of the edge being included at least as many triangles if edges were random, given the size of the endpoints' neighborhoods (smaller is more important)

The normalize parameter determines whether edge scores are normalized.

- none: no normalization is performed
- rank: scores are normalized by neighborhood rank, such that the strongest edge in a node's neighborhood is ranked 1 (asymmetric)
- embeddedness: scores are normalized using the maximum Jaccard coefficient of the top k-ranked neighbors of each endpoint, for all k

The filter parameter determines how edges are filtered based on their (normalized) edge scores.

- threshold: Edges with scores >= s are retained in the backbone
- proportion: Specifies the approximate proportion of edges to retain in the backbone
- degree: Retains each node's d^s most important edges, where d is the node's degree (requires that normalize = "rank")
- disparity: Applies the disparity filter using disparity()

Using escore == "degree" or normalize == "rank" can yield an assymmetric network. When symmetrize == TRUE (default), after applying a filter, the network is symmetrized by such that i-j if i->j or i<-j.

Specific combinations of escore, normalize, filter, and umst correspond to specific sparsification models in the literature, and are available via the following wrapper functions: sparsify.with.skeleton(), sparsify.with.gspar(), sparsify.with.lspar(), sparsify.with.simmelian(), sparsify.with.jaccard(), sparsify.with.meetmin(), sparsify.with.geometric(), sparsify.with.hypergeometric(), sparsify.with.localdegree(), sparsify.with.quadrilateral(). See the documentation for these wrapper functions for more details and the associated citation.

Value

An unweighted, undirected, unipartite graph of class class.

References

Neal, Z. P. (2022). backbone: An R Package to Extract Network Backbones. *PLOS ONE*, *17*, e0269137. doi:10.1371/journal.pone.0269137

Examples

```
 \begin{tabular}{ll} U &--igraph::sbm.game(60, matrix(c(.75,.25,.25,.25,.25,.25,.25,.25,.25),3,3), c(20,20,20)) \\ plot(U) &\#A \ hairball \\ sparse &-- sparsify(U, s = 0.6, escore = "jaccard", normalize = "rank", \\ filter = "degree", narrative = TRUE) \\ plot(sparse) &\#Clearly \ visible \ communities \\ \end{tabular}
```

```
sparsify.with.geometric
```

Extract Goldberg and Roth's (2003) Geometric backbone

Description

sparsify.with.geometric is a wrapper for sparsify() that extracts the geometric backbone described by Goldberg and Roth (2003). It is equivalent to sparsify(escore = "geometric", normalize = "none", filter = "threshold", umst = FALSE).

Usage

```
sparsify.with.geometric(U, s, class = "original", narrative = FALSE)
```

Arguments

U	An unweighted unipartite graph, as: (1) an adjacency matrix in the form of a matrix or sparse Matrix; (2) an edgelist in the form of a two-column dataframe; (3) an igraph object.
S	numeric: Sparsificiation threshold, $0 < s < 1$; larger values yield sparser graphs
class	string: the class of the returned backbone graph, one of c("original", "matrix", "Matrix", "igraph", "edgelist"). If "original", the backbone graph returned is of the same class as \cup .
narrative	boolean: TRUE if suggested text & citations should be displayed.

Value

sparsify.with.gspar 31

References

package: Neal, Z. P. (2022). backbone: An R Package to Extract Network Backbones. *PLOS ONE*, 17, e0269137. doi:10.1371/journal.pone.0269137

model: Goldberg, D. S., & Roth, F. P. (2003). Assessing experimentally derived interactions in a small world. *Proceedings of the National Academy of Sciences, 100*, 4372-4376. doi:10.1073/pnas.0735871100

Examples

```
 \begin{tabular}{ll} $U < -igraph::sbm.game(60, matrix(c(.75,.25,.25,.25,.25,.25,.25,.25,.25),3,3), \ c(20,20,20)) \\ plot(U) \#A \ hairball \\ sparse < -sparsify.with.geometric(U, s = 0.25, narrative = TRUE) \\ plot(sparse) \#Clearly \ visible \ communities \\ \end{tabular}
```

sparsify.with.gspar

Extract Satuluri et al's (2011) G-spar backbone

Description

sparsify.with.gspar is a wrapper for sparsify() that extracts the G-spar backbone described by Satuluri et al. (2011). It is equivalent to sparsify(escore = "jaccard", normalize = "none", filter = "proportion", umst = FALSE).

Usage

```
sparsify.with.gspar(U, s, class = "original", narrative = FALSE)
```

Arguments

U	An unweighted unipartite graph, as: (1) an adjacency matrix in the form of a matrix or sparse Matrix; (2) an edgelist in the form of a two-column dataframe; (3) an igraph object.
S	numeric: Proportion of edges to retain, $0 < s < 1$; smaller values yield sparser graphs
class	string: the class of the returned backbone graph, one of c("original", "matrix", "Matrix", "igraph", "edgelist"). If "original", the backbone graph returned is of the same class as U.
narrative	boolean: TRUE if suggested text & citations should be displayed.

Value

References

package: Neal, Z. P. (2022). backbone: An R Package to Extract Network Backbones. *PLOS ONE*, 17, e0269137. doi:10.1371/journal.pone.0269137

model: Satuluri, V., Parthasarathy, S., & Ruan, Y. (2011, June). Local graph sparsification for scalable clustering. In Proceedings of the 2011 ACM SIGMOD International Conference on Management of data (pp. 721-732). doi:10.1145/1989323.1989399

Examples

```
 \begin{tabular}{ll} $U < -igraph::sbm.game(60, matrix(c(.75,.25,.25,.25,.25,.25,.25,.25,.25),3,3), \ c(20,20,20)) \\ plot(U) \#A \ hairball \\ sparse < -sparsify.with.gspar(U, s = 0.4, narrative = TRUE) \\ plot(sparse) \#Clearly \ visible \ communities \\ \end{tabular}
```

sparsify.with.hypergeometric

Extract Goldberg and Roth's (2003) Hypergeometric backbone

Description

sparsify.with.hypergeometric is a wrapper for sparsify() that extracts the hypergeometric backbone described by Goldberg and Roth (2003). It is equivalent to sparsify(escore = "hypergeometric", normalize = "none", filter = "threshold", umst = FALSE).

Usage

```
sparsify.with.hypergeometric(U, s, class = "original", narrative = FALSE)
```

Arguments

U	An unweighted unipartite graph, as: (1) an adjacency matrix in the form of a matrix or sparse Matrix; (2) an edgelist in the form of a two-column dataframe; (3) an igraph object.
S	numeric: Sparsificiation threshold, $0 < s < 1$; smaller values yield sparser graphs
class	string: the class of the returned backbone graph, one of c("original", "matrix", "Matrix", "igraph", "edgelist"). If "original", the backbone graph returned is of the same class as U.
narrative	boolean: TRUE if suggested text & citations should be displayed.

Value

sparsify.with.jaccard 33

References

package: Neal, Z. P. (2022). backbone: An R Package to Extract Network Backbones. *PLOS ONE*, 17, e0269137. doi:10.1371/journal.pone.0269137

model: Goldberg, D. S., & Roth, F. P. (2003). Assessing experimentally derived interactions in a small world. *Proceedings of the National Academy of Sciences*, 100, 4372-4376. doi:10.1073/pnas.0735871100

Examples

```
U \leftarrow igraph::sbm.game(60, matrix(c(.75,.25,.25,.25,.25,.25,.25,.25,.25,.3,3), c(20,20,20)) plot(U) #A hairball sparse \leftarrow sparsify.with.hypergeometric(U, s = 0.3, narrative = TRUE) plot(sparse) #Clearly visible communities
```

sparsify.with.jaccard Extract Goldberg and Roth's (2003) Jaccard backbone

Description

sparsify.with.jaccard is a wrapper for sparsify() that extracts the jaccard backbone described by Goldberg and Roth (2003). It is equivalent to sparsify(escore = "jaccard", normalize = "none", filter = "threshold", umst = FALSE).

Usage

```
sparsify.with.jaccard(U, s, class = "original", narrative = FALSE)
```

Arguments

U	An unweighted unipartite graph, as: (1) an adjacency matrix in the form of a matrix or sparse Matrix; (2) an edgelist in the form of a two-column dataframe; (3) an igraph object.
S	numeric: Sparsificiation threshold, $0 < s < 1$; larger values yield sparser graphs
class	string: the class of the returned backbone graph, one of c("original", "matrix", "Matrix", "igraph", "edgelist"). If "original", the backbone graph returned is of the same class as U.
narrative	boolean: TRUE if suggested text & citations should be displayed.

Value

References

package: Neal, Z. P. (2022). backbone: An R Package to Extract Network Backbones. *PLOS ONE*, 17, e0269137. doi:10.1371/journal.pone.0269137

model: Goldberg, D. S., & Roth, F. P. (2003). Assessing experimentally derived interactions in a small world. *Proceedings of the National Academy of Sciences*, 100, 4372-4376. doi:10.1073/pnas.0735871100

Examples

```
U \leftarrow igraph::sbm.game(60, matrix(c(.75,.25,.25,.25,.25,.25,.25,.25,.25,.3,3), c(20,20,20)) plot(U) #A hairball sparse \leftarrow sparsify.with.jaccard(U, s = 0.3, narrative = TRUE) plot(sparse) #Clearly visible communities
```

sparsify.with.localdegree

Extract Hamann et al.'s (2016) Local Degree backbone

Description

sparsify.with.localdegree is a wrapper for sparsify() that extracts the local degree backbone described by Hamann et al. (2016). It is equivalent to sparsify(escore = "degree", normalize = "rank", filter = "degree", umst = FALSE).

Usage

```
sparsify.with.localdegree(U, s, class = "original", narrative = FALSE)
```

Arguments

U	An unweighted unipartite graph, as: (1) an adjacency matrix in the form of a matrix or sparse Matrix; (2) an edgelist in the form of a two-column dataframe; (3) an igraph object.
S	numeric: Sparsification exponent, $0 < s < 1$; smaller values yield sparser graphs
class	string: the class of the returned backbone graph, one of c("original", "matrix", "Matrix", "igraph", "edgelist"). If "original", the backbone graph returned is of the same class as U.
narrative	boolean: TRUE if suggested text & citations should be displayed.

Value

sparsify.with.lspar 35

References

package: Neal, Z. P. (2022). backbone: An R Package to Extract Network Backbones. *PLOS ONE*, 17, e0269137. doi:10.1371/journal.pone.0269137

model: Hamann, M., Lindner, G., Meyerhenke, H., Staudt, C. L., & Wagner, D. (2016). Structure-preserving sparsification methods for social networks. *Social Network Analysis and Mining*, 6, 22. doi:10.1007/s1327801603322

Examples

```
 \begin{tabular}{ll} U <- igraph::as.undirected(igraph::sample_pa(60, m = 3), mode = "collapse") \\ plot(U) \#A hairball \\ sparse <- sparsify.with.localdegree(U, s = 0.3, narrative = TRUE) \\ plot(sparse) \#Clearly visible hubs \\ \end{tabular}
```

sparsify.with.lspar

Extract Satuluri et al's (2011) L-spar backbone

Description

sparsify.with.lspar is a wrapper for sparsify() that extracts the L-spar backbone described by Satuluri et al. (2011). It is equivalent to sparsify(escore = "jaccard", normalize = "rank", filter = "degree", umst = FALSE).

Usage

```
sparsify.with.lspar(U, s, class = "original", narrative = FALSE)
```

Arguments

U	An unweighted unipartite graph, as: (1) an adjacency matrix in the form of a matrix or sparse Matrix; (2) an edgelist in the form of a two-column dataframe; (3) an igraph object.
S	numeric: Sparsification exponent, $0 < s < 1$; smaller values yield sparser graphs
class	string: the class of the returned backbone graph, one of c("original", "matrix", "Matrix", "igraph", "edgelist"). If "original", the backbone graph returned is of the same class as U.
narrative	boolean: TRUE if suggested text & citations should be displayed.

Value

sparsify.with.meetmin

References

package: Neal, Z. P. (2022). backbone: An R Package to Extract Network Backbones. *PLOS ONE*, 17, e0269137. doi:10.1371/journal.pone.0269137

model: Satuluri, V., Parthasarathy, S., & Ruan, Y. (2011, June). Local graph sparsification for scalable clustering. In Proceedings of the 2011 ACM SIGMOD International Conference on Management of data (pp. 721-732). doi:10.1145/1989323.1989399

Examples

```
 \begin{tabular}{ll} $U <-i graph::sbm.game(60, matrix(c(.75,.25,.25,.25,.25,.25,.25,.25,.25),3,3), \ c(20,20,20)) \\ plot(U) \#A \ hairball \\ sparse <- sparsify.with.lspar(U, s = 0.6, narrative = TRUE) \\ plot(sparse) \#Clearly \ visible \ communities \\ \end{tabular}
```

sparsify.with.meetmin Extract Goldberg and Roth's (2003) MeetMin backbone

Description

sparsify.with.meetmin is a wrapper for sparsify() that extracts the meetmin backbone described by Goldberg and Roth (2003). It is equivalent to sparsify(escore = "meetmin", normalize = "none", filter = "threshold", umst = FALSE).

Usage

```
sparsify.with.meetmin(U, s, class = "original", narrative = FALSE)
```

Arguments

U	An unweighted unipartite graph, as: (1) an adjacency matrix in the form of a matrix or sparse Matrix; (2) an edgelist in the form of a two-column dataframe; (3) an igraph object.
S	numeric: Sparsificiation threshold, $0 < s < 1$; larger values yield sparser graphs
class	string: the class of the returned backbone graph, one of c("original", "matrix", "Matrix", "igraph", "edgelist"). If "original", the backbone graph returned is of the same class as U.
narrative	boolean: TRUE if suggested text & citations should be displayed.

Value

References

package: Neal, Z. P. (2022). backbone: An R Package to Extract Network Backbones. *PLOS ONE*, 17, e0269137. doi:10.1371/journal.pone.0269137

model: Goldberg, D. S., & Roth, F. P. (2003). Assessing experimentally derived interactions in a small world. *Proceedings of the National Academy of Sciences*, 100, 4372-4376. doi:10.1073/pnas.0735871100

Examples

```
 \begin{tabular}{ll} $U < -igraph::sbm.game(60, matrix(c(.75,.25,.25,.25,.25,.25,.25,.25,.25),3,3), \ c(20,20,20)) \\ plot(U) \#A \ hairball \\ sparse < -sparsify.with.meetmin(U, s = 0.5, narrative = TRUE) \\ plot(sparse) \#Clearly \ visible \ communities \\ \end{tabular}
```

sparsify.with.quadrilateral

Extract Nocaj et al.'s (2015) Quadrilateral Simmelian backbone

Description

sparsify.with.quadrilateral is a wrapper for sparsify() that extracts the quadrilateral Simmelian backbone described by Nocaj et al. (2015). It is equivalent to sparsify(escore = "quadrilateral embeddedness", normalize = "embeddedness", filter = "threshold", umst = TRUE).

Usage

```
sparsify.with.quadrilateral(U, s, class = "original", narrative = FALSE)
```

Arguments

U	An unweighted unipartite graph, as: (1) an adjacency matrix in the form of a matrix or sparse Matrix; (2) an edgelist in the form of a two-column dataframe; (3) an igraph object.
S	numeric: Sparsification exponent, $0 < s < 1$; larger values yield sparser graphs
class	string: the class of the returned backbone graph, one of c("original", "matrix", "Matrix", "igraph", "edgelist"). If "original", the backbone graph returned is of the same class as U.
narrative	boolean: TRUE if suggested text & citations should be displayed.

Value

References

package: Neal, Z. P. (2022). backbone: An R Package to Extract Network Backbones. *PLOS ONE*, 17, e0269137. doi:10.1371/journal.pone.0269137

model: Nocaj, A., Ortmann, M., & Brandes, U. (2015). Untangling the hairballs of multi-centered, small-world online social media networks. *Journal of Graph Algorithms and Applications*, 19, 595-618. doi:10.7155/jgaa.00370

Examples

```
U \leftarrow igraph::sbm.game(60, matrix(c(.75,.25,.25,.25,.25,.25,.25,.25,.25,.3,3), c(20,20,20)) plot(U) #A hairball sparse \leftarrow sparsify.with.quadrilateral(U, s = 0.5, narrative = TRUE) plot(sparse) #Clearly visible communities in a connected graph
```

sparsify.with.simmelian

Extract Nick et al's (2013) Simmelian backbone

Description

sparsify.with.simmelian is a wrapper for sparsify() that extracts the simmelian backbone described by Nick et al. (2013). It is equivalent to sparsify(escore = "triangles", normalize = "embeddedness", filter = "threshold", umst = FALSE).

Usage

```
sparsify.with.simmelian(U, s, class = "original", narrative = FALSE)
```

Arguments

U	An unweighted unipartite graph, as: (1) an adjacency matrix in the form of a matrix or sparse Matrix; (2) an edgelist in the form of a two-column dataframe; (3) an igraph object.
S	numeric: Sparsificiation threshold, $0 < s < 1$; larger values yield sparser graphs
class	string: the class of the returned backbone graph, one of c("original", "matrix", "Matrix", "igraph", "edgelist"). If "original", the backbone graph returned is of the same class as U.
narrative	boolean: TRUE if suggested text & citations should be displayed.

Value

sparsify.with.skeleton 39

References

package: Neal, Z. P. (2022). backbone: An R Package to Extract Network Backbones. *PLOS ONE*, 17, e0269137. doi:10.1371/journal.pone.0269137

model: Nick, B., Lee, C., Cunningham, P., & Brandes, U. (2013, August). Simmelian backbones: Amplifying hidden homophily in facebook networks. In Proceedings of the 2013 IEEE/ACM international conference on advances in social networks analysis and mining (pp. 525-532). doi:10.1145/2492517.2492569

Examples

```
 \begin{tabular}{ll} $U < -igraph::sbm.game(60, matrix(c(.75,.25,.25,.25,.25,.25,.25,.25,.25),3,3), \ c(20,20,20)) \\ plot(U) \#A \ hairball \\ sparse < -sparsify.with.simmelian(U, s = 0.5, narrative = TRUE) \\ plot(sparse) \#Clearly \ visible \ communities \\ \end{tabular}
```

sparsify.with.skeleton

Extract Karger's (1999) skeleton backbone

Description

sparsify.with.skeleton is a wrapper for sparsify() that extracts the skeleton backbone described by Karger (1999), which preserves a specified proportion of random edges. It is equivalent to sparsify(escore = "random", normalize = "none", filter = "proportion", umst = FALSE).

Usage

```
sparsify.with.skeleton(U, s, class = "original", narrative = FALSE)
```

Arguments

U	An unweighted unipartite graph, as: (1) an adjacency matrix in the form of a matrix or sparse Matrix; (2) an edgelist in the form of a two-column dataframe; (3) an igraph object.
S	numeric: Proportion of edges to retain, $0 < s < 1$; smaller values yield sparser graphs
class	string: the class of the returned backbone graph, one of c("original", "matrix", "Matrix", "igraph", "edgelist"). If "original", the backbone graph returned is of the same class as \cup .
narrative	boolean: TRUE if suggested text & citations should be displayed.

Value

40 sparsify.with.skeleton

References

package: Neal, Z. P. (2022). backbone: An R Package to Extract Network Backbones. *PLOS ONE*, 17, e0269137. doi:10.1371/journal.pone.0269137

model: Karger, D. R. (1999). Random sampling in cut, flow, and network design problems. *Mathematics of Operations Research*, 24, 383-413. doi:10.1287/moor.24.2.383

Examples

```
U <- igraph::erdos.renyi.game(60, .5)
plot(U) #A dense graph
sparse <- sparsify.with.skeleton(U, s = 0.25, narrative = TRUE)
plot(sparse) #A sparser graph</pre>
```

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